Calculus/Limits/Exercises

Basic Limit Exercises

1.
$$\lim_{x \to 2} \left[4x^2 - 3x + 1 \right]$$

$$2.\lim_{x\to 5} \left[x^2\right]$$

One-Sided Limits

Evaluate the following limits or state that the limit does not exist.

3.
$$\lim_{x \to 0^{-}} \frac{x^3 + x^2}{x^3 + 2x^2}$$

$$4. \lim_{x \to 7^{-}} \left[|x^2 + x| - x \right]$$

$$5. \lim_{x \to -1^-} \sqrt{1 - x^2}$$

6.
$$\lim_{x \to -1^+} \sqrt{1 - x^2}$$

Two-Sided Limits

Evaluate the following limits or state that the limit does not exist.

$$7. \lim_{x \to -1} \frac{1}{x-1}$$

8.
$$\lim_{x \to 4} \frac{1}{x-4}$$

9.
$$\lim_{x\to 2}\frac{1}{x-2}$$

10.
$$\lim_{x\to -3} \frac{x^2-9}{x+3}$$

11.
$$\lim_{x\to 3} \frac{x^2-9}{x-3}$$

12.
$$\lim_{x \to -1} \frac{x^2 + 2x + 1}{x + 1}$$

13.
$$\lim_{x \to -1} \frac{x^3 + 1}{x + 1}$$

14.
$$\lim_{x \to 4} \frac{x^2 + 5x - 36}{x^2 - 16}$$

15.
$$\lim_{x\to 25} \frac{x-25}{\sqrt{x}-5}$$

16.
$$\lim_{x \to 0} \frac{|x|}{x}$$

17.
$$\lim_{x\to 2} \frac{1}{(x-2)^2}$$

18.
$$\lim_{x\to 3} \frac{\sqrt{x^2+16}}{x-3}$$

19.
$$\lim_{x \to -2} \frac{3x^2 - 8x - 3}{2x^2 - 18}$$

20.
$$\lim_{x\to 2} \frac{x^2 + 2x + 1}{x^2 - 2x + 1}$$

21.
$$\lim_{x\to 3} \frac{x+3}{x^2-9}$$

$$22. \lim_{x \to -1} \frac{x+1}{x^2+x}$$

23.
$$\lim_{x \to 1} \frac{1}{x^2 + 1}$$

24.
$$\lim_{x \to 1} \left[x^2 + 5x - \frac{1}{2 - x} \right]$$

25.
$$\lim_{x \to 1} \frac{x^2 - 1}{x^2 + 2x - 3}$$

26.
$$\lim_{x \to 1} \frac{5x}{x^2 + 2x - 3}$$

Limits to Infinity

Evaluate the following limits or state that the limit does not exist.

$$27. \lim_{x \to \infty} \frac{-x + \pi}{x^2 + 3x + 2}$$

28.
$$\lim_{x \to -\infty} \frac{x^2 + 2x + 1}{3x^2 + 1}$$

29.
$$\lim_{x \to -\infty} \frac{3x^2 + x}{2x^2 - 15}$$

30.
$$\lim_{x \to -\infty} \left[3x^2 - 2x + 1 \right]$$

31.
$$\lim_{x \to \infty} \frac{2x^2 - 32}{x^3 - 64}$$

32.
$$\lim_{x\to\infty} 6$$

33.
$$\lim_{x \to \infty} \frac{3x^2 + 4x}{x^4 + 2}$$

34.
$$\lim_{x \to -\infty} \frac{2x + 3x^2 + 1}{2x^2 + 3}$$

35.
$$\lim_{x \to -\infty} \frac{x^3 - 3x^2 + 1}{3x^2 + x + 5}$$

36.
$$\lim_{x \to \infty} \frac{x^2 + 2}{x^3 - 2}$$

Limits of Piecewise Functions

Evaluate the following limits or state that the limit does not exist.

37. Consider the function

$$f(x) = egin{cases} (x-2)^2 & ext{if } x < 2 \ x-3 & ext{if } x \geq 2 \end{cases}$$

a.
$$\lim_{x o 2^-}f(x)$$

b.
$$\lim_{x o 2^+}f(x)$$

c.
$$\lim_{x o 2} f(x)$$

38. Consider the function

$$g(x) = egin{cases} -2x+1 & ext{if } x \leq 0 \ x+1 & ext{if } 0 < x < 4 \ x^2+2 & ext{if } x \geq 4 \end{cases}$$

a.
$$\lim_{x o 4^+}g(x)$$

b.
$$\lim_{x o 4^-} g(x)$$

c.
$$\lim_{x o 0^+} g(x)$$

	$\lim_{x o 0^-}g(x)$
	$\lim_{x o 0} g(x)$
f.	$\lim_{x o 1} g(x)$

39. Consider the function

$$h(x) = egin{cases} 2x - 3 & ext{if } x < 2 \ 8 & ext{if } x = 2 \ -x + 3 & ext{if } x > 2 \end{cases}$$

a. $\lim_{x o 0} h(x)$			
b. $\lim_{x o 2^-} h(x)$			

c.
$$\lim_{x o 2^+} h(x)$$

d. $\lim_{x o 2} h(x)$

External Links

- Limits 1 exercise at Khan Academy (http://www.khanacademy.org/exercise/limits_1)
- Limits 2 exercise at Khan Academy (http://www.khanacademy.org/exercise/limits_2)

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